

# ICAM



INTERDISCIPLINARY CENTER FOR APPLIED MATHEMATICS



VIRGINIA POLYTECHNIC INSTITUTE  
AND STATE UNIVERSITY

Blacksburg, Virginia 24061-0531

**Air Force Workshop on Optimal Design and Control**

**Final Technical Report on AFOSR Grant**

**F49620-97-1-0264**

for the period 1 April 1997 - 31 December 1997

by

John A. Burns

Eugene M. Cliff

Center for Optimal Design And Control  
Interdisciplinary Center for Applied Mathematics  
Virginia Polytechnic Institute and State University

<b>ICAM REPORT 98-03-01</b>
-----------------------------

Prepared for the:    Air Force Office of Scientific Research  
Code NM  
110 Duncan Avenue, Suite B115  
Bolling AFB, DC 20332-0001

# REPORT DOCUMENTATION PAGE

Form Approved  
OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.

1. AGENCY USE ONLY (Leave blank)		2. REPORT DATE 6 March 1998		3. REPORT TYPE AND DATES COVERED Technical Final Report, 1 April 1997 - 31 December 1997	
4. TITLE AND SUBTITLE  Air Force Workshop on Optimal Design and Control				5. FUNDING NUMBERS  (G) F49620-97-1-0264	
6. AUTHOR(S)  J.A. Burns					
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES) Interdisciplinary Center for Applied Mathematics Wright House, West Campus Drive Virginia Polytechnic Institute and State University Blacksburg, Virginia 24061-0531				AFRL-SR-BL-TR-98- 0277	
9. SPONSORING / MONITORING AGENCY NAME(S) AND ADDRESS(ES) Air Force Office of Scientific Research Code NM 110 Duncan Avenue, Suite B115 Bolling AFB, DC 20332				10. SPONSORING / MONITORING AGENCY REPORT NUMBER  19980331 063	
11. SUPPLEMENTARY NOTES					
12a. DISTRIBUTION / AVAILABILITY STATEMENT  Unlimited				12b. DISTRIBUTION CODE	
13. ABSTRACT (Maximum 200 words)  This report contains a summary and highlights of the work funded by the Air Force under AFOSR Grant F49620-97-1-0264, titled " Air Force Workshop on Optimal Design and Control ". This effort was conducted by the Air Force Center for Optimal Design and Control (CODAC), during the period 1 April 1997 - 31 December 1997. The Center planned, organized and ran a workshop in Washington, DC from 30 September through 3 October 1997. The workshop was attended by sixty-six participants with thirty-six technical presentations.  The objectives of the workshop included an assessment of current research efforts in optimal design, an evaluation of Air Force needs and identification of future directions in optimal design. The speakers, including twenty invited leading researchers, covered a variety of topics including: Sensitivity Equation Methods, Adjoint Methods, Automatic Differentiation, Optimization Theory and Algorithms and Engineering Design Applications. Twenty-two of the technical papers have been assembled into a Proceeding volume, to be published by Birkhauser-Boston. A second volume assessing the state-of-the-art and future directions will also be published by Birkhauser-Boston					
14. SUBJECT TERMS  Optimal Design, Sensitivity Analysis, Adjoint Methods, Automatic Differentiation				15. NUMBER OF PAGES 29	
				16. PRICE CODE	
17. SECURITY CLASSIFICATION OF REPORT Unclassified	18. SECURITY CLASSIFICATION OF THIS PAGE Unclassified	19. SECURITY CLASSIFICATION OF ABSTRACT Unclassified	20. LIMITATION OF ABSTRACT UL		

## Summary

This Grant provided partial support for a workshop on Computational Methods for Optimal Design and Control that was held in Washington, DC, 30 September – 3 October 1997. The basic objectives of the proposed workshop were

1. to assess the current status of research in optimal design as it applies to Air Force problems,
2. to bring together the diverse group of researchers in this area in order to share and compare the different approaches to inverse design and
3. to provide an evaluation of Air Force needs and future directions in computational tools for optimal design.

To meet these objectives approximately twenty internationally recognized leaders were invited to present status reports on their basic research programs. With the addition of contributed talks a total of thirty-six presentations were made. In addition, each attendee was asked to provide a brief hand-written summary of issues and challenges. This information was used to identify future directions and to draft a report analyzing the challenges posed by future Air Force problems. Two volumes have been produced as a result of the workshop. One volume is a proceedings containing twenty-two of the scientific papers. The second volume provides an assessment of the state of the art and an analysis of future directions in the field. Both volumes are being published by *Birkhauser - Boston*. The Proceedings volume is in-press and will appear in April 1998. The front-matter from this volume is included as an Appendix. The Future Directions volume is in editorial review and will be available later in the year.

# **1 Introduction and Overview**

Many of the most challenging engineering design applications currently facing the Air Force and the aerospace industry may be formulated as optimal design or inverse problems. These applications include, but are not limited to, structural optimization, nozzle and shape design for wind tunnel testing, wing/body design, inverse design for improved stealth, general shape optimization for flow management, combustion and high speed flows. It is this universal range of applications that has generated a demand for new optimization-based computational tools. The widespread demand for such tools has generated a tremendous surge in research on computational methods for optimal design. During the past decade, this work has produced numerous new methods and lead to the development of a wide variety of computational algorithms.

In order to address these fundamental questions, the workshop brought together sixty-three participants from a wide spectrum of research disciplines including: optimization theory, control theory, computational mechanics, structural dynamics, computer science, computational fluid dynamics, numerical analysis and computational physics.

The Conference Program is included as Appendix A and a list of participants is included as Appendix B. The front-matter of the Proceedings volume, to be published by *Birkhauser - Boston*, is included as a final Appendix.

# **2 Technical Areas**

The thirty-six presentations at the Workshop covered a variety of themes including:

- Sensitivity Equation Methods
- Adjoint Methods
- Automatic Differentiation
- Optimization Theory and Algorithms
- Engineering Design Applications

## 2.1 Sensitivity Equation Methods

There are a variety of approaches to the formulation and solution of engineering design problems. We concentrate here on a class of problems which can be formulated as mathematical optimization problems. When used as a paradigm for engineering design, the state sensitivities (derivative of the state with respect to the design parameters) play two key roles. They provide gradient information for the optimization algorithm and sensitivity information for analysis of a particular design. Therefore, efficient computation of accurate sensitivities is a major requirement of any design tool.

## 2.2 Adjoint Methods

For many applications the adjoint equation approach is an attractive alternative to the SEM for the computation of gradients. While the adjoint equations are used for various distributed optimal control problems, many issues are still subject to active research. One issue that arises repeatedly is the issue of consistency and adjointness: In many applications, discretizations of the infinite dimensional adjoint equation are not the adjoint equations of the discretized problem and vice versa. Additional research issues arise that concern the correct mathematical setting of the problem, formulation of the adjoint equation, in particular boundary conditions for the adjoint, and the existence of the adjoints.

## 2.3 Automatic Differentiation

In many applications the direct or analysis problem results in software package capable of predicting the system's performance for given values of the design parameters. In such setting it is natural to adopt a computational viewpoint that focuses on exploiting the existing simulation code. Thus the basic idea in automatic differentiation is to produce an auxiliary computer code that will compute the sensitivity of the original code to changes in data. The idea is very attractive in many industrial applications wherein complex *legacy codes* have been developed for the direct problem. OSR has previously sponsored a workshop in this area in January 1991.

## **2.4 Optimization Theory and Algorithms**

Design problems can be formulated as optimization problems in a variety of ways, among these the black-box-formulation and the all-at-once formulation are extreme points. In many cases the smoothness (or lack thereof) of the cost and constraint functionals is a key issue. For smooth problems sequential quadratic programming (SQP) methods with trust-region strategies are among the preferred approaches. However, many *legacy* codes for simulating the behavior of engineering systems include features which induce non-smooth dependence on design parameters. Thus, a number of contributors addressed such issues. Finally, in many engineering disciplines one has a spectrum of available analysis models/tools. These may range from simple inexpensive database-interpolation methods, to sophisticated CFD simulation codes. Several speakers addressed issues related to model-management in the context of optimization.

## **2.5 Engineering Design Applications**

The motivation for the tool-development described above stems from a variety of applications in aerospace design. One aspect of these problems is their multidisciplinary nature. In a comprehensive design for transport aircraft, for example, structural, aerodynamic, propulsive and flight-control requirements must each be considered. Several speakers addressed these concepts.

## **Workshop Program**



**Tuesday Morning, 30 September 1997**

08:00 - 08:45	Registration
08:45 - 09:00	Welcome: Salon A
	<b>Session TU-AM: Salon A</b> <b>Session Chair: Major Scott Schreck</b>
09:00 - 09:45	Roland Glowinski University of Houston <i>Some Fundamental Issues in Optimal Design/Shape Optimization</i>
09:45 - 10:30	Ekkehard Sachs Universitat Trier <i>New Numerical Methods in Optimal Control</i>
10:30 - 11:00	Coffee Break: Salon A
11:00 - 11:45	Max Gunzburger Iowa State University <i>Sensitivities and Adjointns in Computational Methods for Optimal Flow Control</i>

**Tuesday Afternoon, 30 September 1997**

	<b>Session TU-PM: Salon A</b> <b>Session Chair: Eugene M. Cliff</b>
13:15 - 14:00	Andrew Conn T.J. Watson Research Center, IBM <i>Recent Progress in Unconstrained            Nonlinear Optimization Without Derivatives</i>
14:00 - 14:45	Thomas Coleman Cornell University <i>Automatic Differentiation is NOT Automatic            (When Applied to Inverse Problems in Optimal Design)</i>
14:45 - 15:15	Coffee Break: Salon A
15:15 - 16:00	Gal Berkooz BEAM Technologies, Inc <i>Optimization in Real World Engineering Design:            Needs and Opportunities</i>
16:00 - 16:45	Jason Speyer University of California, Los Angeles <i>Robust Reduced-Order Controller of            Transitional Boundary Layers</i>
16:45 - 17:15	Discussion

**Wednesday Morning, 1 October 1997**

	<b>Session WE-AM-1: Salon B</b> <b>Session Chair: John A. Burns</b>
08:00 - 08:45	Jaroslav Haslinger Charles University <i>Fictitious Domain Approaches and Global Optimization Methods in Shape Optimization</i>
08:45 - 09:30	Nicholas Zabaras Cornell University <i>Sensitivity Analyses and Adjoint Method Algorithms for the Design of Material Processes</i>
09:30 - 10:00	Coffee Break: Salon A
	<b>Session WE-AM-2: Salon B</b> <b>Session Chair: Belinda King</b>
10:00 - 10:30	Eyal Arian ICASE <i>MDO-A Mathematical View Point</i>
10:30 - 11:00	Matthias Heinkenschloss Rice University <i>Interior point SQP Methods for Distributed Control Problems</i>
11:00 - 11:30	Josip Loncaric ICASE <i>Sensor/Actuator Placement Via Optimal Distributed Control of Exterior Stokes Flow</i>
11:30 - 12:00	Arun Verma Cornell University <i>Automatic Differentiation and MATLAB Interface Toolbox (ADMIT)</i>

### Wednesday Afternoon, 1 October 1997

	<b>Session WE-PM: Salon B</b> <b>Session Chair: John Dennis</b>
13:30 - 14:15	Allen Tannenbaum University of Minnesota <i>Visual Information in a Feedback Loop: A Control/Computer Vision Synthesis</i>
14:15 - 15:00	Eugene Cliff Virginia Polytechnic Institute and State University <i>An Overview of Research at the Center for Optimal Design And Control</i>
15:00 - 15:30	Coffee Break: Salon A
15:30 - 16:15	Jean-Paul Zolesio Institut Non Lineaire de Nice <i>Shape Differential Equations</i>
16:15 - 16:45	Discussion

### Thursday Morning, 2 October 1997

	<b>Session TH-AM: Salon B</b> <b>Session Chair: Terry Herdman</b>
08:00 - 08:45	John Dennis Rice University <i>Optimization Using Surrogate Objectives</i>
08:45 - 09:30	Anthony Patera Massachusetts Institute of Technology <i>Fast Bounds for Partial Differential Equation Outputs</i>
09:30 - 10:00	Coffee Break: Salon A
10:00 - 10:45	Andrew Godfrey AeroSoft, Inc. <i>Using Sensitivities for Flow Analysis</i>
10:45 - 11:30	Karl Kunisch KFU Graz <i>Numerical Optimal Control for Navier Equations</i>

**Thursday Afternoon, 2 October 1997**

	<b>Session TH-PM 1: Salon B</b> <b>Session Chair: Bernard Grossman</b>
13:15 - 13:45	Robert Lewis NASA Langley Research Center <i>Sensitivity Calculations and the Adjoint Equations from a Nonlinear Programming Perspective</i>
13:45 - 14:15	Ajit Shenoy Virginia Polytechnic Institute and State University <i>An All-At-Once Approach to Airfoil Design</i>
14:15 - 14:45	Dominique Pelletier Ecole Polytechnique de Montreal <i>On Computational Issues in Using Adaptive FEM and the Sensitivity Equation Method</i>
14:45 - 15:15	Coffee Break: Salon A
	<b>Session TH-PM 2: Salon B</b> <b>Session Chair: Marc Jacobs</b>
15:15 - 15:45	Jeff Borggaard Cornell University <i>On Optimal Design in Forced Convection</i>
15:45 - 16:15	John Otto Massachusetts Institute of Technology <i>A Surrogate-Pareto Approach to Shape Optimization: Level-Set Based Geometry Description</i>
16:15 - 16:45	Belinda King Oregon State University <i>An Optimal Design Approach to the Construction of Practical Feedback Controllers</i>
16:45 - 17:15	Duane Knill Virginia Polytechnic Institute and State University <i>Efficient Implementation of Euler Solutions for Supersonic Aerodynamic Predictions in Multidisciplinary HSCT Design</i>

**Friday Morning, 3 October 1997**

	<b>Session FR-AM-1: Salon B</b> <b>Session Chair: Max Gunzburger</b>
08:00 - 08:45	C.T. Kelley North Carolina State University <i>The Simplex Gradient and Noisy Optimization Problems</i>
08:45 - 09:30	Bernard Grossman Virginia Polytechnic Institute and State University <i>Multidisciplinary Design Optimization of Advanced Aircraft</i>
09:30 - 10:00	Coffee Break: Salon A
	<b>Session FR-AM-2: Salon B</b> <b>Session Chair: Ekkehard Sachs</b>
10:00 - 10:30	Martin Berggren FFA, The Aeronautical Research Institute of Sweden <i>Optimal Disturbances in Boundary Layers</i>
10:30 - 11:00	Dawn Stewart Virginia Polytechnic Institute and State University <i>Projection Methods for Accurate Computation of Design Sensitivities</i>
11:00 - 11:30	Paul Hovland Argonne National Laboratory <i>Automatic Differentiation and Navier-Stokes Computations</i>
11:30 - 12:00	Jean-Francois Héту National Research Council of Canada <i>Optimization of Industrial Forming Processes: Issues and Challenges</i>

**Friday Afternoon, 3 October 1997**

	<b>Session FR-PM: Salon B</b> <b>Session Chair: Nicholas Zabarar</b>
13:30 - 14:15	Ilan Kroo Stanford University <i>Optimal Design of Aerospace Systems– Architectures and Applications</i>
14:15 - 15:00	Antony Jameson Stanford University <i>Optimum Design of Airplane Wings in Transonic Viscous Flow</i>
15:00 - 15:30	Coffee Break: Salon A
16:00 - 16:45	H.T. Banks North Carolina State University <i>Identification Problems in Electro-Magnetics</i>
16:45 - 17:15	Closing Session: Dr. John Burns

## **List of Participants**



*Workshop on Optimal Design and Control*  
*Crystal Gateway Marriott*  
*September 30 - October 3, 1997*

Arian, Eyal  
ICASE  
Mail Stop 403  
6 North Dryden Street  
NASA Langley Research Center  
Hampton, VA 23681-0001  
757-864-2208  
arian@icase.edu

Banks, H.T.  
North Carolina State University  
324 Harrelson Hall  
CRSC, Box 82  
Raleigh, NC 27695  
919-515-3968  
htbanks@crsc1.math.ncsu.edu

Berggren, Martin  
FFA, The Aeronautical Research  
Institute of Sweden  
Computational Aerodynamics  
Department  
P.O. Box 11021  
S-161 11 Bromma, Sweden  
46-8-6341071  
bnm@ffa.se

Berkooz, Gal  
BEAM Technologies, Inc.  
110 North Cayuga Street  
Ithaca, NY 14850  
607-273-4367  
gb@beamtech.com

Boggs, Paul  
National Institute of Standards  
Mathematical and Computational  
Sciences Division  
Gaithersburg, MD 208999  
301-975-3816  
boggs@nist.gov

Borggaard, Jeffrey  
Cornell University  
287 Upson Hall  
Mechanical and Aerospace  
Engineering  
Ithaca, NY 14853  
607-255-8270  
borggajt@fred.mae.cornell.edu

Bradley, Beth  
University of Louisville  
Department of Mathematics  
Louisville, KY 40292  
502-852-6826  
mebrad01@homer.louisville.edu

Burns, John  
Virginia Polytechnic Institute and  
State University  
Interdisciplinary Center for  
Applied Mathematics  
Blacksburg, VA 24061-0531  
540-231-7667  
burns@icam.vt.edu

Camphouse, Chris  
Virginia Polytechnic Institute and  
State University  
Interdisciplinary Center for  
Applied Mathematics  
Blacksburg, VA 24061-0531  
540-231-7667  
rcamphou@math.vt.edu

Cifuentes, Paula  
Virginia Polytechnic Institute and  
State University  
Northern Virginia Graduate Center  
7054 Haycock Road  
Falls Church, VA 22043-2311  
703-538-8395  
pcifuent@sun.icam.vt.edu

Cliff, Eugene  
Virginia Polytechnic Institute and  
State University  
Interdisciplinary Center for  
Applied Mathematics  
Blacksburg, VA 24061-0531  
540-231-7667  
cliff@icam.vt.edu

Coleman, Thomas  
Cornell University  
Dept. of Computer Science  
725 Eng. and Theory Center Bldg  
Ithaca, NY 14853-3801  
607-255-9203  
coleman@cs.cornell.edu

Conn, Andrew  
T.J. Watson Research Center, IBM  
P.O. Box 218  
Yorktown Heights, NY 10598-  
0218  
914-945-1589  
arconn@watson.ibm.com

Dennis, John  
Rice University  
CAAM-MS 134  
6100 Main Street  
Houston, TX 77005  
713-527-4094 713-527-4094  
dennis@rice.edu

Feijoo, Gonzalo R.  
Stanford University  
Department of Mechanical  
Engineering  
Division of Mechanics and  
Computation  
Durand Building Room 262  
Stanford, CA 94305  
650-723-1142  
grfeij@leland.stanford.edu

Gao, Dong-Ming  
National Research Council Canada  
75 de Mortagne Blvd.  
Boucherville  
Quebec, Canada  
514-641-5030  
dong-ming.gao@mkc.ca

Giesy, Daniel P.  
NASA Langley Research Center  
Guidance and Control Branch  
MS 161  
Hampton, VA 23681  
757-864-4006  
d.p.giesy@larc.nasa.gov

Gilmore, Paul  
Tektronix, Inc.  
Color Printing and Imaging  
Division  
26600 S.W. Parkway  
P.O. Box 1000, M/S 63-424  
Wilsonville, OR 97070  
503-685-2288  
paulgi@pogo.wv.tek.com

Glowinski, Roland  
University of Houston  
Department of Mathematics  
4800 Calhoun Road  
Houston, TX 77204-3476  
713-743-3473  
roland@math.uh.edu

Godfrey, Andrew  
AeroSoft, Inc.  
1872 Pratt Drive  
Suite 1275  
Blacksburg, VA 24060  
540-231-8117  
godfrey@aerosft.com

Grossman, Bernard  
Virginia Polytechnic Institute and  
State University  
Department of Aerospace and Ocean  
Engineering  
Blacksburg, VA 24061-0203  
540-231-6611  
grossman@apollo.aoe.vt.edu

Gunzburger, Max  
Iowa State University  
Department of Mathematics  
400 Carver Hall  
Ames, IA 50011-2064  
515-294-1752  
gunzburg@iastate.edu

Haslinger, Jaroslav  
Charles University  
Faculty of Mathematics and Physics  
KFK MFF UK  
Ke Karlovu 5  
121 16 Prague 2, CZECH  
REPUBLIC  
420-2-21911312  
haslin@apollo.karlov.mff.cuni.cz

Heinkenschloss, Matthias  
Rice University  
Department of Computational and  
Applied Mathematics  
6100 Main Street  
Houston, TX 77005-1892  
713-285-5176  
heinken@caam.rice.edu

Henningson, Dan  
FFA Aeronautical Research  
Institute of Sweden  
Box 11021  
S-16111 Bromma, Sweden  
46-8-6341270  
hnd@ffa.se

Herdman, Terry  
Virginia Polytechnic Institute and  
State University  
Interdisciplinary Center for  
Applied Mathematics  
Blacksburg, VA 24061-0531  
540-231-7667  
herdman@icam.vt.edu

Herling, William  
Boeing Defense and Space Group  
Aerodynamics Technology  
P.O. Box 3707  
M.S.4A-38  
Seattle, WA 98124-2207  
206-662-0056  
wwh3507@hef.ds.boeing.com

Hetu, Jean-Francois  
National Research Council of  
Canada  
Industrial Materials Institute  
75 de Mortagne  
Boucherville, Quebec  
Canada J4B 6Y4  
phone:  
514-641-5364  
jean-francois.hetu@nrc.ca

Holland, Charles  
Air Force Office of Scientific  
Research  
110 Duncan Avenue  
Suite B115  
Bolling AFB, 20332-0001  
holland@afosr.af.mil

Hovland, Paul  
Argonne National Laboratory  
Mathematics and Computer Science  
Division  
Building 221  
9700 S. Cass Avenue  
Argonne, IL 60439  
630-252-6384  
hovland@mcs.anl.gov

Hulsing, Kevin  
Virginia Polytechnic Institute and  
State University  
Interdisciplinary Center for  
Applied Mathematics  
Blacksburg, VA 24061-0531  
540-231-7667  
hulsing@icam.vt.edu

Jacobs, Marc  
Air Force Office of Scientific  
Research  
110 Duncan Avenue  
Suite B115  
Bolling AFB, 20332-0001  
marc@stealth.afosr.af.mil

Jameson, Antony  
Stanford University  
Department of Aeronautics and  
Astronautics  
Durand 279  
Stanford, CA 94305  
415-725-6208  
jameson@gorilla.stanford.edu

Kearsley, Anthony  
NIST  
Math and Computer Science  
Division  
Gaithersburg, MD 20899-0001  
301-975-6103  
ajk@cam.nist.gov

Kelley, Carl T.  
North Carolina State University  
Department of Mathematics  
Box 8205  
Raleigh, NC 27695-8205  
919-515-7163  
tim\_kelley@ncsu.edu

King, Belinda  
Oregon State University  
Department of Mathematics  
Corvallis, OR 97331  
541-737-4686  
bbking@math.orst.edu

Knill, Duane  
Virginia Polytechnic Institute and  
State University  
215 Randolph Hall  
Aerospace and Ocean Engineering  
Blacksburg, VA 24061-0203  
540-231-3550  
knill@aoe.vt.edu

Kroo, Ilan  
Stanford University  
Department of Aeronautics and  
Astronautics  
Stanford, CA 94305-4035  
415-723-2994  
kroo@leland.stanford.edu

Kunisch, Karl  
University of Graz  
Institute fuer Mathematik  
Heinrichstrasse 36  
A 8010 Graz, Austria  
0043-316-380-5162  
kunisch@kfunigraz.ac.at

Lewis, Robert  
ICASE  
Mail Stop 403  
NASA Langley Research Center  
Hampton, VA 23681-0001  
757-864-2190  
buckaroo@icase.edu

Limache, Alejandro  
Virginia Polytechnic Institute and  
State University  
Interdisciplinary Center for  
Applied Mathematics  
Blacksburg, VA 24061-0531  
540-231-7667  
alimach@icam.vt.edu

Loncaric, Josip  
ICASE  
Mail Stop 403  
NASA Langley Research Center  
Hampton, VA 23681-0001  
757-864-2192  
josip@icase.edu

Maghami, Peiman G.  
NASA Langley Research Center  
Mail Stop 161  
Hampton, VA 23681-0001  
757-864-4039  
p.g.maghami@larc.nasa.gov

Malhotra, Manish  
Stanford University  
PO Box 7169  
Stanford, CA 94309  
650-723-8595  
maam-sun2.stanford.edu

Moerder, Dan  
NASA Langley Research Center  
Mail Stop 161  
Hampton, VA 23681  
757-864-6495  
dmoerder@lambic.larc.nasa.gov

Nash, Stephen  
George Mason University  
Operations Research Dept  
Fairfax, VA 22030  
703-993-1678  
snash@gmu.edu

Otto, John C.  
M.I.T.  
Department of Aeronautics and  
Astronautics  
Fluids Lab Room 3-243  
77 Massachusetts Avenue  
Cambridge, MA 02139  
617-253-0229  
jo@andrei.mit.edu

Patera, Anthony  
M.I.T.  
Department of Mechanical  
Engineering  
Room 3-264  
77 Massachusetts Avenue  
Cambridge, MA 02139  
617-253-8122  
patera@mit.edu

Pelletier, Dominique  
Ecole Polytechnique de Montreal  
PO Box 6079  
Station A  
Montreal, Canada H3C 3A7  
514-340-4711, ext. 4102  
dp@galerkin.meca.polymtl.ca

Roetman, Fritz  
Boeing Defense and Space Group  
Aerodynamics Technology  
P.O. Box 3707  
MS 4A-38  
Seattle, WA 98124-2207  
206-662-0063  
ernest.l.roetman@boeing.com

Rubio, Diana  
North Carolina State University  
Center for Research in Scientific  
Computation  
Box 8205  
Raleigh, NC 27695  
919-515-3310  
adrubio@eos.ncsu.edu

Sachs, Ekkehard  
Universität Trier  
FB IV-Mathematik  
54296 Trier, Germany  
49-651-201-3474  
sachs@uni-trier.de

Schreck, Scott  
Air Force Office of Scientific  
Research/NM  
110 Duncan Avenue  
Suite B115  
Bolling AFB, DC 20332-8050  
202-767-7902  
scott.schreck@afosr.af.mil

Shenoy, Ajit  
Virginia Polytechnic Institute and  
State University  
Interdisciplinary Center for  
Applied Mathematics  
Blacksburg, VA 24061-0531  
540-231-7667  
shenoy@icam.vt.edu

Speyer, Jason  
University of California, Los  
Angeles  
Mechanical and Aerospace  
Engineering Department  
Box 951597  
Los Angeles, CA 90095-1597  
310-206-4451  
speyer@seas.ucla.edu

Stanley, Lisa  
Virginia Polytechnic Institute and  
State University  
Interdisciplinary Center for  
Applied Mathematics  
Blacksburg, VA 24061-0531  
540-231-7667  
stanley@math.vt.edu

Starnes, Craig  
Booz, Allen & Hamilton, Inc.  
2231 Crystal Drive  
Arlington, VA 22202  
703-902-4026  
starnes-craig@bah.com

Stewart, Dawn  
Virginia Polytechnic Institute and  
State University  
Interdisciplinary Center for  
Applied Mathematics  
Blacksburg, VA 24061-0531  
540-231-7667  
stewartd@icam.vt.edu

Tannenbaum, Allen  
University of Minnesota  
200 Union Street S.E.  
Department of Electrical  
Engineering  
Minneapolis, MN 55455  
612-625-6395  
tannenba@ee.umn.edu

Torczon, Virginia  
College of William and Mary  
Dept. of Computer Science  
P.O. Box 8795  
Williamsburg, VA 23187-8795  
757-221-3460  
va@cs.wm.edu

Verma, Arun  
Cornell University  
716 Rhodes Hall  
Ithaca, NY 14853  
phone:  
607-254-8807  
verma@cs.cornell.edu

Zabaras, Nicholas  
Cornell University  
Sibley School of Mechanical and  
Aerospace Engineering  
188 Rhodes Hall  
Ithaca, NY 14853-3801  
607-255-9104  
njz1@cornell.edu

Zolésio, Jean-Paul  
Institut Non Linéaire de Nice  
2004 Route des Lucioles  
BP 93 06902 Sophia Antipolis  
Cedex, France  
336-09-57-88-94  
jean.paul.esio@inria.sophia.fr

## **Proceedings Volume – Frontmatter**

# COMPUTATIONAL METHODS FOR OPTIMAL DESIGN AND CONTROL

*Proceedings of the AFOSR Workshop  
on Optimal Design and Control  
Arlington, Virginia  
30 September–3 October, 1997*

Jeff Borggaard, John Burns,  
Eugene Cliff and Scott Schreck  
Editors

Jeff Borggaard  
Center for Optimal Design and Control  
Sibley School of Mechanical and Aerospace Engineering  
Cornell University  
Ithaca, NY 14853, USA  
jborggaard@na-net.ornl.gov

John Burns  
Center for Optimal Design and Control  
Interdisciplinary Center for Applied Mathematics  
Virginia Tech  
Blacksburg, VA 24061-0531, USA  
burns@icam.vt.edu

Eugene Cliff  
Center for Optimal Design and Control  
Interdisciplinary Center for Applied Mathematics  
Virginia Tech  
Blacksburg, VA 24061-0531, USA  
cliff@icam.vt.edu

Scott Schreck  
Air Force Office of Scientific Research  
Bolling Air Force Base  
Washington, DC 20332-8050, USA  
scott.schreck@afosr.af.mil



## CONTENTS

Preface . . . . .	vii
Contributors . . . . .	xi
Optimal Disturbances in Boundary Layers <i>P. Andersson, M. Berggren and D. Henningson</i> . . . . .	1
MDO - A Mathematical View Point <i>E. Arian</i> . . . . .	27
Optimization Using Surrogate Objectives on a Helicopter Test Example <i>A. Booker, J. Dennis Jr., P. Frank, D. Serafini and V. Torczon</i> . . . . .	49
Observations in Adaptive Refinement Strategies for Optimal Design <i>J. Borggaard and D. Pelletier</i> . . . . .	59
The Simplex Gradient and Noisy Optimization Problems <i>D. Bortz and C. T. Kelley</i> . . . . .	77
Adjoint-Based Methods in Aerodynamic Design Optimization <i>E. Cliff, M. Heinkenschloss and A. Shenoy</i> . . . . .	91
Semi-Automatic Differentiation <i>T. Coleman, F. Santosa and A. Verma</i> . . . . .	113
Robust Reduced-Order Controller of Transitional Boundary Layers <i>L. Cortelezzi and J. Speyer</i> . . . . .	127
Modern Optimization Methods for Structural Optimization under Flutter Constraints <i>M. Fahl and E. Sachs</i> . . . . .	137
On Shape Optimization and Related Issues <i>R. Glowinski and J. He</i> . . . . .	151
Using Sensitivities for Flow Analysis <i>A. Godfrey</i> . . . . .	181
Sensitivities in Computational Methods for Optimal Flow Control <i>M. Gunzburger</i> . . . . .	197

Fictitious Domain Approaches in Shape Optimization <i>J. Haslinger</i> . . . . .	237
Process Modeling and Optimization: Issues and Challenges <i>J.-F. Hetu, F. Ilinca and D. Pelletier</i> . . . . .	249
Automatic Differentiation and Navier-Stokes Computations <i>P. Hovland, B. Mohammadi and C. Bischof</i> . . . . .	265
Numerical Computation of Sensitivities and the Adjoint Approach <i>R. Lewis</i> . . . . .	285
Sensor/Actuator Placement via Optimal Distributed Control of Exterior Stokes Flow <i>J. Lončarić</i> . . . . .	303
Fast Bounds for Outputs of Partial Differential Equations <i>M. Paraschivoiu, J. Peraire, Y. Maday and A. Patera</i> . . . . .	323
A Comparison of Local and Global Projections in Design Sensitivity Computations <i>L. Stanley and D. Stewart</i> . . . . .	361
Gradients, Curvature, and Visual Tracking <i>A. Tannenbaum and A. Yezzi, Jr.</i> . . . . .	375
Adjoint Methods for Inverse Free Convection Problems with Application to Solidification Processes <i>N. Zabaras</i> . . . . .	391
Shape Differential Equation with a Non Smooth Field <i>J.-P. Zolésio</i> . . . . .	427

## PREFACE

This volume contains the proceedings of the Second International Workshop on Optimal Design and Control, held in Arlington, Virginia, 30 September–3 October, 1997. The First Workshop was held in Blacksburg, Virginia in 1994. The proceedings of that meeting also appeared in the Birkhauser series on Progress in Systems and Control Theory and may be obtained through Birkhauser.

These workshops were sponsored by the Air Force Office of Scientific Research through the Center for Optimal Design and Control (CODAC) at Virginia Tech. The meetings provided a forum for the exchange of new ideas and were designed to bring together diverse viewpoints and to highlight new applications. The primary goal of the workshops was to assess the current status of research and to analyze future directions in optimization based design and control. The present volume contains the technical papers presented at the Second Workshop. More than 65 participants from 6 countries attended the meeting and contributed to its success.

It has long been recognized that many modern optimal design problems are best viewed as variational and optimal control problems. Indeed, the famous problem of determining the body of revolution that produces a minimum drag nose shape in hypersonic flow was first proposed by Newton in 1686. Optimal control approaches to design can provide theoretical and computational insight into these problems. This volume contains a number of papers which deal with computational aspects of optimal control.

The workshop was a gathering of engineers and mathematicians actively involved in innovative research in control and optimization, with an emphasis placed on optimal design problems governed by partial differential equations. Many difficulties arise when trying to implement approximation techniques for these problems. These difficulties range from computational issues, such as the accuracy, ease and efficiency of state/function and gradient calculations, to concerns about integrating calculations from several subdisciplines. For example, contributions concerning gradient calculations can be loosely broken into three categories: (i) Automatic Differentiation, (ii) Adjoint Methods and (iii) Sensitivity Equations Methods.

In many cases, a detailed solution of the full physics-based state equations (partial differential equations or large systems of ordinary differential equations) is expensive. However, reduced order models with varying levels of validity can often be used to develop optimal design strategies. Several articles describe techniques for managing models in optimization algorithms. Model management is also considered for the case where different disciplines must be integrated. Model uncertainty caused by coarse approximations of partial differential equations or by obtaining function evaluations through experiment can introduce unacceptable noise in the design objective function. Convergence of optimization algorithms for problems with model uncertainty is discussed by various contributors.

Many important optimal design applications can be formulated as shape optimization problems. Shape optimization leads to additional difficulties and often requires the development of special techniques to address complex theoretical and computational issues. These difficulties range from theoretical considerations involving the development of proper mathematical framework for the discussion of shape derivatives, to computational methods for efficient calculation, or elimination of mesh gradients. Sensitivity equation methods and fictitious domain approaches to these problems are found in various articles on shape optimization.

The diverse background and experience of the participants, ranging from academia, to industry, to government laboratories, lead to a variety of techniques to address these difficulties. Overall, it is clear that there has been significant progress in the development of new computational and mathematical tools for optimal design and control. Moreover, these tools are being applied to very complex systems and have important applications to aerodynamic design, fluid flows, materials processing, inverse design and feedback control. On the other hand, there are many theoretical and practical issues that have not been resolved, and when resolved, could lead to revolutionary advances in design and control methodology. During the workshop the participants submitted position papers that identified these issues and suggested future research directions to address these difficult problems. The conclusions based on these suggestions will appear in a follow-up volume.

Finally, we would like to acknowledge the efforts of the Organizing Committee, the graduate students at Virginia Tech and the staff at ICAM. In particular, special thanks goes to Dr. Bernard Grossman, Melissa Chase and Sydney Crowder for their help in putting together the interesting and informative workshop that led to these proceedings. We also gratefully acknowledge the support of the Air Force Office of Scientific Research for funding the workshop under AFOSR grants F49620-97-1-0264 and F49620-96-1-0329.

Jeff Borggaard, John Burns,  
Eugene Cliff and Scott Schreck  
*Blacksburg*  
*December 1997*

## CONTRIBUTORS

*Paul Andersson* – FFA, the Aeronautical Research Institute Sweden, Computational Aerodynamics Department, P.O Box 11021, S-161 11 Bromma, Sweden.

*Eyal Arian* – Institute for Computer Applications in Science and Engineering, Mail Stop 403, NASA Langley Research Center, Hampton, VA 23681.

*Martin Berggren* – FFA, the Aeronautical Research Institute Sweden, Computational Aerodynamics Department, P.O Box 11021, S-161 11 Bromma, Sweden.

*Christian Bischof* – Mathematics and Computer Science Division, Argonne National Laboratory, 9700 S. Cass Avenue, Argonne, IL 60439-4844.

*Andrew Booker* – Mathematics & Engineering Analysis, Boeing Information Support Services.

*Jeff Borggaard* – Sibley School of Mechanical and Aerospace Engineering, Upson Hall, Cornell University, Ithaca, NY 14853.

*David Bortz* – North Carolina State University, Department of Mathematics, Center for Research in Scientific Computation, Box 8205, Raleigh, NC 27695-8205.

*Eugene Cliff* – Center for Optimal Design and Control, Interdisciplinary Center for Applied Mathematics, Virginia Tech, West Campus Drive, Blacksburg, VA 24061-0531.

*Thomas Coleman* – Computer Science Department and Center for Applied Mathematics, Cornell University, Ithaca, NY 14850.

*Luca Cortelezzi* – Department of Mechanical and Aerospace Engineering and Department of Mathematics, University of California, Los Angeles, CA 90095.

*John Dennis, Jr.* – Department of Computational and Applied Mathematics, Center for Research on Parallel Computation, Rice University, Houston, TX.

*M. Fahl* – FB IV - Mathematik, Universität Trier, 54286 Trier, Germany.

*Paul Frank* – Mathematics & Engineering Analysis Boeing Information Support Services.

- Roland Glowinski* – University of Houston, Department of Mathematics, Houston, TX 77204-3476.
- Andrew Godfrey* – Aerosoft, Inc., 1872 Pratt Drive, Ste. 1275, Blacksburg, VA 24060.
- Max Gunzburger* – Department of Mathematics, Iowa State University, Ames, IA 50011-2064.
- Jaroslav Haslinger* – Charles University, Prague.
- Jiwen He* – University of Houston, Department of Mathematics, Houston, TX 77204-3476.
- Matthias Heinkenschloss* – Department of Computational and Applied Mathematics, Rice University, Houston, TX.
- Dan Henningson* – FFA, the Aeronautical Research Institute Sweden, Computational Aerodynamics Department, P.O. Box 11021, S-161 11 Bromma, Sweden.
- Jean-François Hétu* – Industrial Materials Institute, National Research Council Canada, 75, de Mortagne, Boucherville, QC, Canada J4B 6Y4.
- Paul Hovland* – Mathematics and Computer Science Division, Argonne National Laboratory, 9700 S. Cass Avenue, Argonne, IL 60439-4844.
- Florin Ilina* – Industrial Materials Institute, National Research Council Canada, 75, de Mortagne, Boucherville, QC, Canada J4B 6Y4.
- C. Tim Kelley* – North Carolina State University, Department of Mathematics, Center for Research in Scientific Computation, Box 8205, Raleigh, NC 27695-8205.
- Robert Michael Lewis* – Institute for Computer Applications in Science and Engineering, Mail Stop 403, NASA Langley Research Center, Hampton, VA 23681-0001.
- Josip Lončarić* – Institute for Computer Applications in Science and Engineering, Mail Stop 403, NASA Langley Research Center, Hampton, VA 23681-0001.
- Yvon Maday* – Laboratoire d'Analyse Numérique, Université Pierre and Marie Curie (Paris VI).
- Bijan Mohammadi* – University of Montpellier II and INRIA, Math. Dept, CC51, 34095 Montpellier Cedex 5, France.

- Marius Paraschivoiu* – Department of Mechanical Engineering, Massachusetts Institute of Technology, 77 Massachusetts Avenue, Cambridge, MA 02139.
- Anthony Patera* – Department of Mechanical Engineering, Massachusetts Institute of Technology, 77 Massachusetts Avenue, Cambridge, MA 02139.
- Dominique Pelletier* – Department of Mechanical Engineering, Ecole Polytechnic de Montréal, C.P. 6079, Succ. A, Montréal, QC, Canada H3C 3A7.
- Jaime Peraire* – Department of Aeronautics and Astronautics, Massachusetts Institute of Technology, 77 Massachusetts Avenue, Cambridge, MA 02139.
- Ekkehard Sachs* – FB IV - Mathematik, Universität Trier, 54286 Trier, Germany.
- Fadil Santosa* – School of Mathematics, University of Minnesota, Minneapolis, MN 55455.
- David Serafini* – Department of Computational and Applied Mathematics, Center for Research on Parallel Computation, Rice University, Houston, TX.
- Ajit Shenoy* – Department of Mathematics, Iowa State University, Ames, IA 50011-2064.
- Jason Speyer* – Department of Mechanical and Aerospace Engineering, University of California, Los Angeles, CA 90095.
- Lisa Stanley* – Center for Optimal Design and Control, Interdisciplinary Center for Applied Mathematics, Virginia Tech, Blacksburg, VA 24061-0531.
- Dawn Stewart* – Center for Optimal Design and Control, Interdisciplinary Center for Applied Mathematics, Virginia Tech, Blacksburg, VA 24061-0531.
- Allen Tannenbaum* – Department of Electrical Engineering, University of Minnesota, Minneapolis, MN 55455.
- Virginia Torczon* – Computer Science Department, College of William & Mary, Williamsburg, VA
- Arun Verma* – Computer Science Department, Cornell University, Ithaca, NY 14850.
- Anthony Yezzi, Jr.* – Department of Electrical Engineering, University of Minnesota, Minneapolis, MN 55455.
- Nicholas Zabaras* – Sibley School of Mechanical and Aerospace Engineering, 188 Frank H. T. Rhodes Hall, Cornell University, Ithaca, NY 14853-3801.
- Jean-Paul Zolésio* – Institut Non Linéaire de Nice, CNRS, 1361 Route des Lucioles, 06904 Sophia Antipolis Cédex, France.